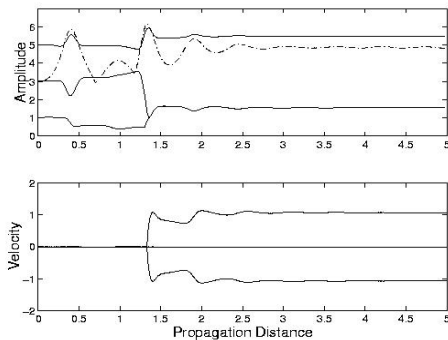


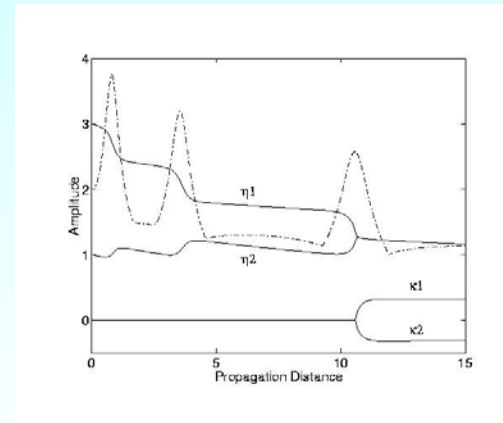
High-order soliton splitting (II)

- Deeper understanding of high-order soliton fission can be obtained by studying the **evolution of the discrete spectrum of the scattering problem** associated with the NSE [2], thus treating nonparaxiality as a perturbation.
- **Focusing** stages introduce strong **shifts** in the **energy eigenvalues**. The **splitting** takes place when two of the constituent solitons become **degenerate**: a pair of equal energy and opposite transverse velocity escaping solitons is produced.



- * The figures show the evolution of the **discrete energy** (upper figure) and transverse velocity (lower figure) **eigenvalues**. Dashed-dotted lines shows the beam peak amplitude. The beam parameters are the same as those from the previous page ($N=3$ and $\kappa=0.005$).

- The same kind of behaviour is found in **other situations** where the evolution of **high-order solitons** is studied in the presence of **perturbations of the NSE** [5].
 - * The figure shows the evolution of the discrete energy (η_1, η_2) and transverse velocity (κ_1, κ_2) eigenvalues of a $N=2$ soliton in the presence of **two-photon absorption** ($K=0.01$). Dashed-dotted lines show the peak amplitude of the beam.



- This bifurcation structure of the soliton eigenvalues found in high-order soliton splitting appears to be of a general nature and suggests the existence of an **exclusion principle** for solitons and, thus, a **fermion-like** character of solitons particles.